A First-Order Interpreter for Knowledge-based Golog based on Exact Progression and Limited Reasoning

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- Based on closed world assumption (CWA), dynamic CWA, or domain closure assumption (DCA)
- Query evaluation based on regression, with decreasing efficiency as the length of action sequences grows
- Online, offline or a combination
  - search operator for guarding successful execution
  - planning operator for improving efficiency



# Proper<sup>+</sup> Knowledge Bases [Lakemeyer and Levesque, 02]

### Definition

A first-order KB equivalent to a possibly infinite set of clauses

#### Example

$$\begin{aligned} &\forall x.x \neq y \supset \neg on(x,y) \lor \neg clear(y), \quad \forall x. \neg on(x,x) \\ &\forall x,y,z.y \neq z \supset \neg on(x,y) \lor \neg on(x,z) \\ &\forall x.x \neq A \land x \neq D \supset clear(x) \end{aligned}$$

#### [Liu, Lakemeyer & Levesque, 04]

proposed a logic of limited belief  $\mathcal{SL}$  and showed  $\mathcal{SL}$ -based reasoning with proper<sup>+</sup> KBs is decidable.

#### [Liu & Lakemeyer, 09]

showed for local-effect actions and proper  $^+$  KBs, progression is not only first-order definable but also efficiently computable.



An interpreter based on exact progression and limited reasoning

- Handle first-order incomplete information in the form of proper<sup>+</sup> KBs
- Implemented progression and limited reasoning by grounding based on unique name assumption
- The search operator returns a conditional plan
- The planning operator calls a modern planner when local complete information is available



## Implementing Progression and Evaluation by Grounding

- We first implemented algorithms by Liu, Lakemeyer and Levesque, but the implementations were not efficient
- We considered implementation via grounding, but there are infinitely many individuals
- The trick is to use an appropriate number of them as representatives of those not mentioned by the KB



#### Proper<sup>+</sup> Blocks World

 $\forall x.x \neq y \supset \neg on(x,y) \lor \neg clear(y), \ \forall x.x \neq A \land x \neq B \supset clear(x)$ 

The width of the proper<sup>+</sup>KB above is 2, so we intrduce 2 representatives,  $u_1$  and  $u_2$ .

#### Grounding (brute-force)

$$\neg on(A, B) \lor \neg clear(B), \ \neg on(A, u_1) \lor \neg clear(u_1), \\ \neg on(A, u_2) \lor \neg clear(u_2), \neg on(B, A) \lor \neg clear(A), \\ \neg on(B, u_1) \lor \neg clear(u_1), \neg on(B, u_2) \lor \neg clear(u_2) \dots \\ clear(u_1), clear(u_2)$$



### Extended Grounding

### ${}^{\scriptsize \hbox{\tiny I\!S}}$ It should be extended to describe new individuals explicitly too.

Original KB with  $u_1$  and  $u_2$  as representatives

$$\neg on(u_1, u_2), \ \neg on(u_1, A), \ \neg on(u_1, B), \ \neg on(A, u_1), \ \neg on(B, u_1), \ clear(u_1), \ \neg on(u_1, u_1), \dots$$

<sup>IEF</sup> When an action mentions a new individual  $c_1$ , we add the following to the original KB:

#### Extension with new individual $c_1$

$$\neg on(c_1, u_2), \neg on(u_1, c_1), \neg on(c_1, A), \neg on(c_1, B),$$
  
 $\neg on(A, c_1), \neg on(B, c_1),$   
 $clear(c_1), \neg on(c_1, c_1), \ldots$ 



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#### Local-Effect Actions

only change the truth value of fluent atoms with arguments mentioned by the actions

Influenced Atoms of  $\alpha = move(B, A, c_1)$ 

 $on(B,A,s), on(A,c_1,s), clear(A,s), clear(c_1,s)$ 

#### Progression of a ground KB

- extend the ground KB if needed
- 2 add successor state axioms instantiated wrt influenced atoms
- I forget the influenced atoms via resolution

#### Theorem

Progression here is equivalent to that in [Liu & Lakemeyer, 09].



- We perform unit propagation over a ground KB
- For clause evaluation
  - $eval(\phi(d_1,\ldots,d_n)) \to eval(\phi(u_1,\ldots,u_n))$ , for  $d_1,\ldots,d_n$ not mentioned by KB and  $u_1,\ldots,u_n$  as representatives
  - check if  $\phi(u_1,\ldots,u_n)$  is subsumed by a clause in the KB
- Others are reduced to clause evaluation recursively, e.g.
  - $\operatorname{eval}(\eta \lor \psi) {\longrightarrow} \operatorname{eval}(\eta)$  or  $\operatorname{eval}(\psi)$  returns true
  - ${\rm eval}(\exists x\psi) \longrightarrow {\rm eval}(\psi(x/d))$  returns true for some d in a particular finite domain

#### Theorem

Evaluation here is equivalent to that in [Liu et al., 04] at  $\mathcal{B}_0$  level.



### Implemented in Prolog

• with evaluation and progression implemented in C

### Search Operator $\Sigma(\delta)$

- Looking ahead to ensure that nondeterministic choices are resolved to guarantee the successful completion of  $\delta$
- $\bullet\,$  Sensing actions allowed in  $\delta$  and a conditional plan is returned
- Automatically branching wrt sensing results, not relying on special branching actions specified by the programmer



- Based on the work of [Baier, Fritz & McIlraith, 07]
- au explicitly specifies the domain of all related individuals
- Local complete information: for any  $P(\vec{c})$  related to  $\delta$ ,  $P(\vec{c}) \in KB$  or  $\neg P(\vec{c}) \in KB$
- No sensing actions are allowed in  $\delta$
- Calling a modern planner to return a sequence of actions, improving efficiency and ensuring soundness and completeness
- A planner can be called multiple times efficiently because progression maintains the current KB



## Experimental Results for Wumpus World ( $8 \times 8$ , 3000)

Prob	Gold	IMP	Reward	Moves	Time	Calls
10%	1412	695	437	33	0.670	16
15%	890	917	275	22	0.430	11
20%	567	1171	175	14	0.254	7
30%	263	1581	82	6	0.112	3
40%	182	1924	58	3	0.064	2



## An Example Program Execution in the Blocks World

#### Proper<sup>+</sup> Initial KB

$$\begin{aligned} &\forall x.x \neq A \land x \neq B \land x \neq C \land x \neq D \supset clear(x), \\ &\forall x, y.x \neq y \supset \neg on(x,y) \lor \neg clear(y), \quad \forall x. \neg on(x,x), \\ &\forall x, y.x \neq y \supset \neg on(x,y) \lor \neg on(y,x), \ldots \end{aligned}$$

very little knowledge about the exact configuration

Actions: move(x, y, z),  $sense\_clear(x)$ ,  $sense\_on(x, y)$ 

Goal: make clear a list of blocks: A, B, C, D



## Conclusions

- Implemented a Golog interpreter based on exact progression of first-order incomplete information
- Implemented limited reasoning, no CWA, DCWA or DCA, but only unique name assumption and DCWA on knowledge
- Implemented progression and evaluation via grounding with theoretical foundation
- A planning problem is generated dynamically each time the planner is called during a single execution task
- Search operator returns a conditional plan not relying on special branching actions

Future Work

 $\bullet$  Implement limited reasoning at the  $\mathcal{B}_1$  level

